

$$a) \int_{-b}^b |\psi|^2 dx = 1 \quad \text{or} \quad A^2 \int_{-b}^b e^{-2\lambda|x|} dx = 1$$

$$\text{or } 2A^2 \int_0^b e^{-2\lambda x} dx = 1 \quad \text{put } 2\lambda x = y.$$

$$\Rightarrow 2\lambda dx = dy$$

$$x=0, y=0, x=b, y=2\lambda b$$

Our integral is $2A^2 \int_0^{\infty} \frac{e^{-y}}{2\lambda} dy = 1$ or

$$\frac{A^2}{\lambda} (-e^{-y})_0^{\infty} = 1 \quad \text{or}$$

$$-\frac{A^2}{\lambda} (0-1) = 1 \quad \text{or} \quad \boxed{A^2 = \lambda}$$

$$b) \langle x \rangle = \int_{-b}^b (\sqrt{\lambda})^2 x \cdot e^{-2\lambda|x|} dx$$

$$= (\sqrt{\lambda})^2 \int_{-b}^b x e^{-2\lambda|x|} dx$$

$$= (\sqrt{\lambda})^2 \left[\int_{-b}^0 x e^{+2\lambda x} dx + \int_0^b x e^{-2\lambda x} dx \right]$$

The $[\]$ vanish as the 2 integrals are negative of each other.

$$c) \langle x^2 \rangle = (\sqrt{\lambda})^2 \left[\int_{-b}^0 x^2 e^{+2\lambda x} dx + \int_0^b x^2 e^{-2\lambda x} dx \right]$$

$$= (\sqrt{\lambda})^2 \left[-\int_0^b y^2 e^{-2\lambda y} dy + \int_0^b x^2 e^{-2\lambda x} dx \right]$$

$$= 2(\sqrt{\lambda})^2 \int_0^b x^2 e^{-2\lambda x} dx$$