

# $D^0 \rightarrow K_S \pi^0$ and $D^0 \rightarrow K_L \pi^0$ decay rate asymmetry

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## Charm Meeting

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## $D^0 \rightarrow K_S \pi^0$ and $D^0 \rightarrow K_L \pi^0$ decay rate asymmetry

- Decay rate asymmetry in  $D^0 \rightarrow K_S \pi^0$  and  $K_L \pi^0$ , where does it come from?
  - $D^0$  decays occur through  $\bar{K}^0 \pi^0$ (CF mode) and  $K^0 \pi^0$ (DCS mode)
    1. The contributions reflect in the decay width expressions
$$\Gamma_{D^0 \rightarrow K_S \pi^0} = \frac{1}{2} \Gamma_{CF} - (\sqrt{\Gamma_{CF}} \sqrt{\Gamma_{DCS}}) \cos(\delta_{CF} - \delta_{DCS}) + \frac{1}{2} \Gamma_{DCS}$$
$$\Gamma_{D^0 \rightarrow K_L \pi^0} = \frac{1}{2} \Gamma_{CF} + (\sqrt{\Gamma_{CF}} \sqrt{\Gamma_{DCS}}) \cos(\delta_{CF} - \delta_{DCS}) + \frac{1}{2} \Gamma_{DCS}$$
    2. the asymmetry can then be written as
$$A = \frac{(\Gamma_{D^0 \rightarrow K_S \pi^0}) - (\Gamma_{D^0 \rightarrow K_L \pi^0})}{(\Gamma_{D^0 \rightarrow K_S \pi^0}) + (\Gamma_{D^0 \rightarrow K_L \pi^0})} \simeq -2\sqrt{\frac{\Gamma_{DCS}}{\Gamma_{CF}}} \cos(\delta_{CF} - \delta_{DCS}) \simeq \tan^2 \theta_C \simeq \mathcal{O}(5\%)$$
- Physics Motivation. refer [ Physics Letters B 505(2001)94-106 ]
  - this asymmetry gives valuable information on  $\delta = \delta_{CF} - \delta_{DCS}$ 
    1.  $\delta$  is strong interaction phase difference between CF and DCS decay amplitudes
    2. in  $SU(3)$  invariance implies  $\delta = 0$
    3. theoretical calculations for other  $\delta$ 's predicted values both in 1st and 2nd quadrant
    4. sign of experimentally obtained asymmetry can confirm which quadrant it should lie in
- Experimental Situation. Previous measurement at Belle in summer 2001
  - $A = 0.06 \pm 0.05(stat) \pm 0.05(syst)$  using  $23.6 fb^{-1}$

## Strategy for the Analysis

- Central points of this analysis
  - Asymmetry is calibrated against reconstruction efficiencies from  $D^0 \rightarrow (K_S \pi^-) \pi^+$  and  $D^0 \rightarrow (K_L \pi^-) \pi^+$
  - 1.  $K^{*-} (K_S \pi^- \text{ or } K_L \pi^-)$  decays to  $\bar{K}^0$  only,  $K_S \pi^-$  and  $K_L \pi^-$  decay 1:1
  - The signal in all 4 decays is extracted by employing  $D^{*+} \rightarrow D^0 \pi_{slow}^+$ 
    1. since  $D^0$  mass is used as constraint for  $K_L$  reconstruction
    2. signal for all 4 decays can be referred by either  $D^{*+}$  or  $D^0 \rightarrow K_S \pi^0$  etc
  - For calibration purposes we assume factorizability of efficiencies (tested in MC)
    1.  $\epsilon^{D^{*+}}(p_1, p_2, \dots) = \epsilon^1(p_1) \times \epsilon^2(p_2) \times \dots$ , 1,2 etc refer to the final state particles
    2. only  $K_S/K_L$  relative efficiency matters, taken from data in calibration modes
  - All yields are measured in bins of  $K^0$  momenta ( $p$ )
    - reduces bias due to  $K_L$  efficiency as it rapidly increases with momenta
    - $A(p) = \frac{\eta_{K_L \pi}^{rec}(p) - r(p) \times \eta_{K_S \pi}^{rec}(p)}{\eta_{K_L \pi}^{rec}(p) + r(p) \times \eta_{K_S \pi}^{rec}(p)}$ , averaged over  $p$

$$1. \quad \eta' s = \text{yields}, \quad r(p) \equiv \frac{\epsilon_{K_L \pi}(p)}{\epsilon_{K_S \pi}(p)} \equiv \frac{\epsilon_{K_L \pi \pi}(p)}{\epsilon_{K_S \pi \pi}(p)} = \frac{\eta_{K_L \pi \pi}^{rec}(p)}{\eta_{K_S \pi \pi}^{rec}(p)} : (K_L/K_S) \text{ relative efficiency}$$

## Data Sample used

- 100,000 Signal MC events for each mode produced by `evtgen`
  - generator → **b20040727-1143** library
  - gsim → **b20030807-1600** library
  - analysis → **b20040727-1143** library
  - $e^+ e^- \rightarrow c\bar{c} \rightarrow frag \rightarrow D^{*+}$ , inclusive by 'inclusive particle type' in `evtgen`
    1. Produces atleast 1  $D^{*+}$  in the event
    2.  $D^{*+} \rightarrow D^0 \pi_{slow}^+$  and decay of  $D^0 \rightarrow$  all 4 modes by 'user decay' table
  - charge conjugate modes not added yet

## Reconstruction, Event Selection and Fitting

- $\pi^0$  from mdst-pio
- $K_S$  from mdst-vee2
  - $dr > 0.25\text{cm}$ ,  $d\phi < 0.1\text{rad}$ ,  $dz < 1\text{cm}$
  - $0.486\text{GeV} < M_{K_S} < 0.510\text{GeV}$  in  $D \rightarrow K_S \pi$
  - $0.491\text{GeV} < M_{K_S} < 0.504\text{GeV}$  in  $D \rightarrow K_S \pi\pi$
- $K_L$  from mdst-klong
  - Detector gives only  $K_L$  direction
  - $M_{D^0}$  and  $M_{K_L}$  is fixed to PDG value and kinematics is solved for  $p_{K_L}$
  - This is a quadratic equation
  - $\frac{-b - (\sqrt{b^2 - 4ac})}{2a}$  is always +ve, currently chosen solution
  - A choice of the solutions is also being studied
- $K^{*-}$  mass cuts
  - $(0.752, 1.032)$  GeV in  $K_L$  mode,  $(0.750, 1.000)$  GeV in  $K_S$  mode

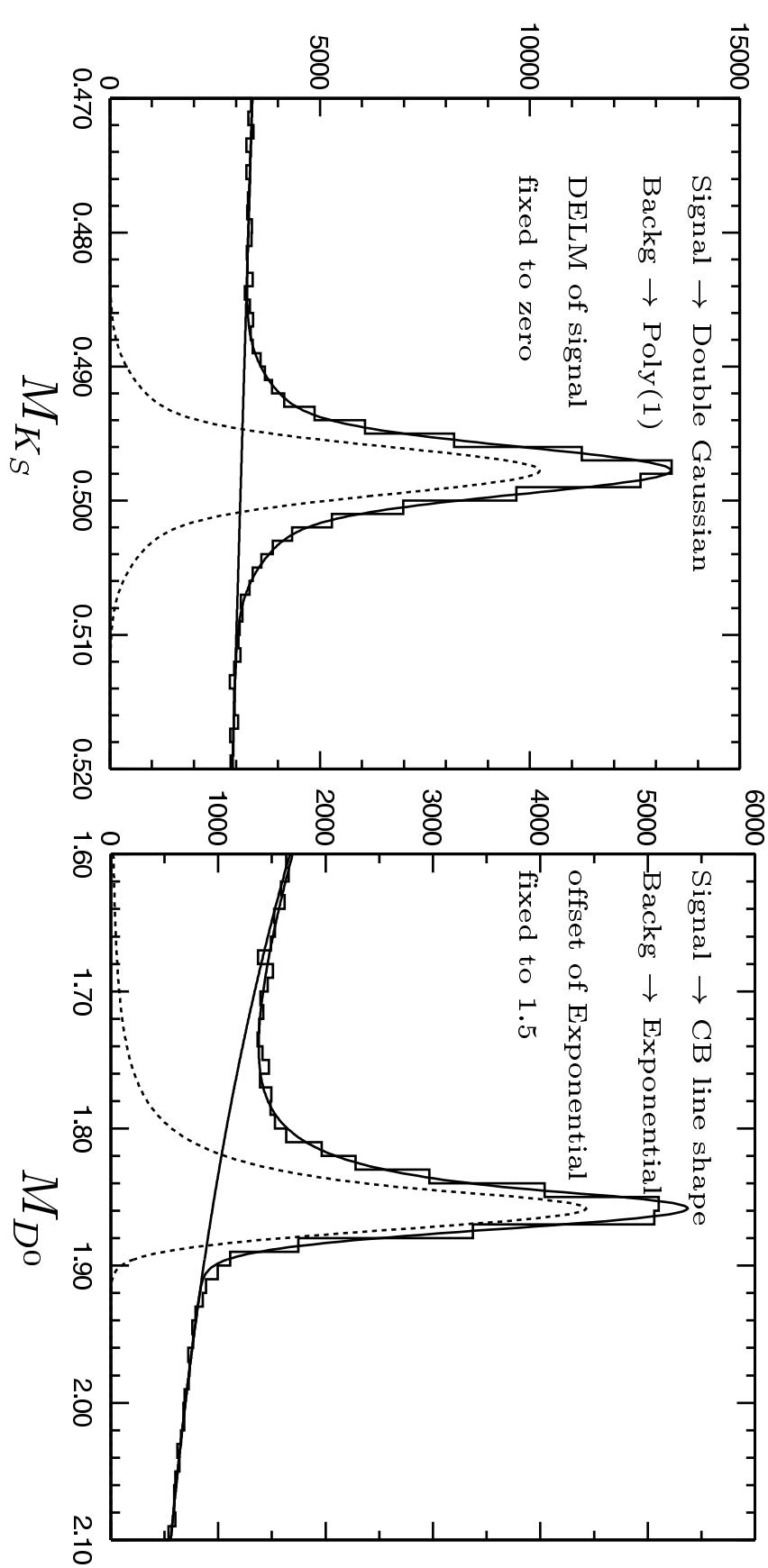
- $D^0$  mass window cuts and constraints
  - (1.75, 1.90) GeV for  $K_S \pi^0$  mode  
(1.852, 1.878) GeV for  $K_S \pi\pi$   
fixed to PDG value for  $K_L$  modes

- $D^{*+}$

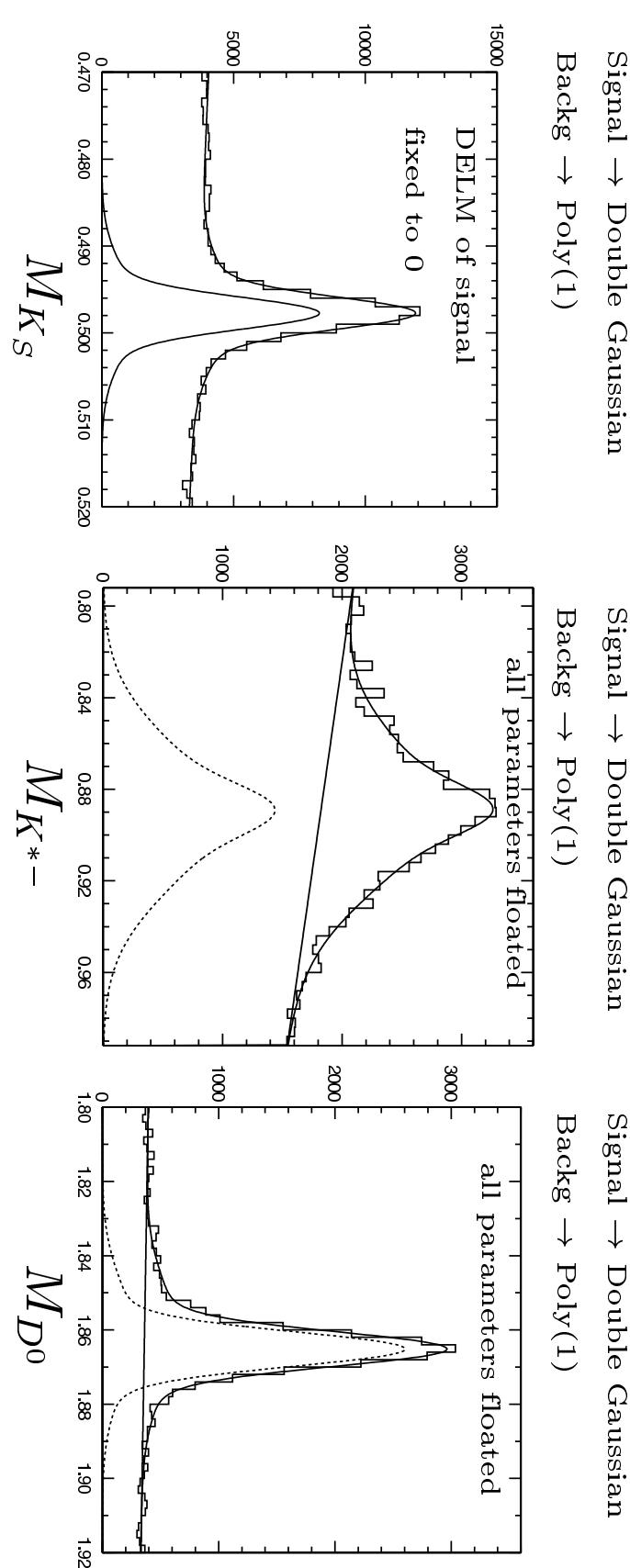
- 3  $\sigma$  cuts on  $M_{D^{*+}}$  for  $K_L$  modes
- $0.144\text{GeV} < \delta M < 0.147\text{GeV}$  for  $D \rightarrow K_S \pi$  mode  
 $0.143\text{GeV} < \delta M < 0.148\text{GeV}$  for  $D \rightarrow K_S \pi\pi$  mode

where  $\delta M = M_{D^{*+}} - M_{D^0}$

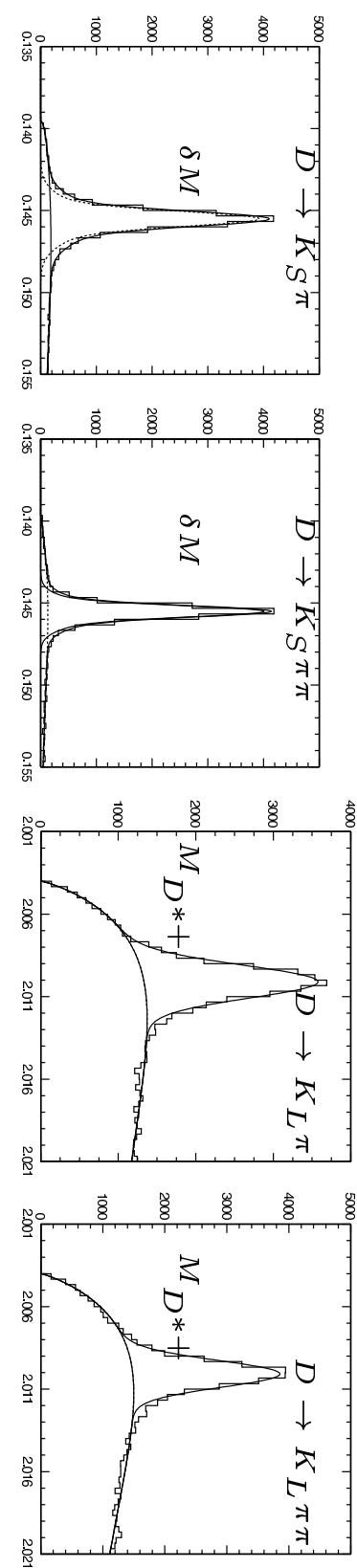
## Reconstruction of $D^0 \rightarrow K_S \pi^0$



## Reconstruction of $D^0 \rightarrow K_S \pi^+ \pi^-$



## Signal shapes for 4-modes



- $\delta M$ , Signal  $\rightarrow$  Double Gaussian

Backg  $\rightarrow$  Threshold function : offset fixed to 0.1396 GeV(PDG)

- $M_{D^*+}$ , Signal  $\rightarrow$  Gaussian

Backg  $\rightarrow$  Threshold function : offset fixed to 2.004 GeV

- Threshold function :

`NORM*(X-OFFSET)**POWER*EXP(COEFF1*(X-OFFSET)+COEFF2*(X-OFFSET)**2)`

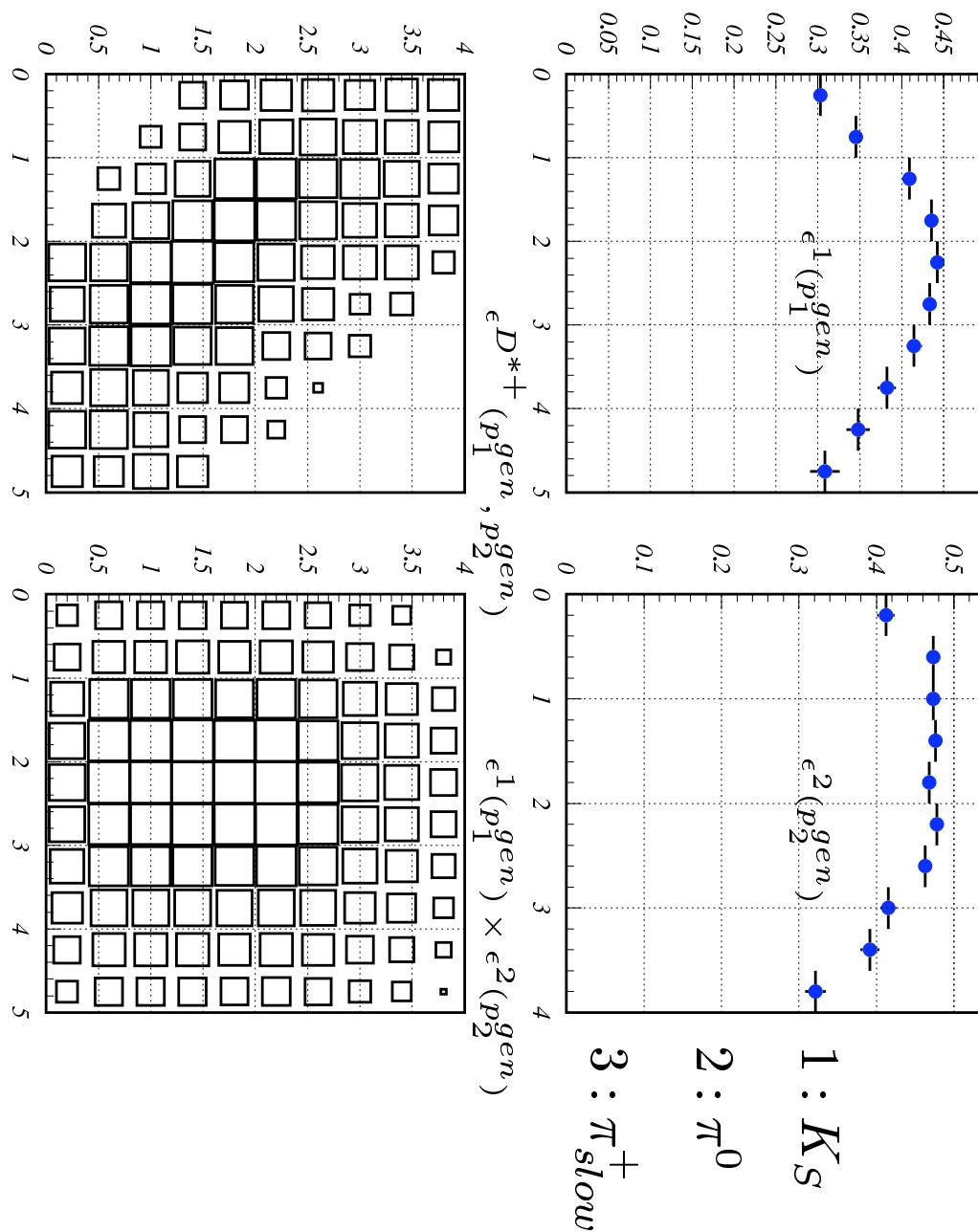
## Reconstruction efficiencies and assumption of factorizability $\epsilon^{D^{*+}}(p_1, p_2, \dots) = \epsilon^1(p_1) \times \epsilon^2(p_2) \times \dots$

- Efficiency study is done in momentum bins to validate factorizability assumption
- To match reconstructed info with MC truth
  - get-hepevt() function is used for  $K_S$ ,  $\pi^0$  and angular cuts for  $K_L$  matching
- Plot the generated lab momenta
  - Count the matching number of events reconstructed in each bin
  - This gives 1d efficiencies as function of momenta eg  $\epsilon^1(p_1)$  etc
- Scatter plot the generated lab momenta pair wise
  - Count the matching number of  $D^{*+}$  events reconstructed in each 2d bins
  - This gives efficiency of  $D^{*+}$  as function of 2 momenta eg  $\epsilon^{D^{*+}}(p_1, p_2)$
- plot  $\epsilon^1(p_1)$ ,  $\epsilon^2(p_2)$ ,  $\epsilon^{D^{*+}}(p_1, p_2)$  and  $\epsilon^1(p_1) \times \epsilon^2(p_2)$ 
  - compare  $\epsilon^{D^{*+}}(p_1, p_2)$  and  $\epsilon^1(p_1) \times \epsilon^2(p_2)$

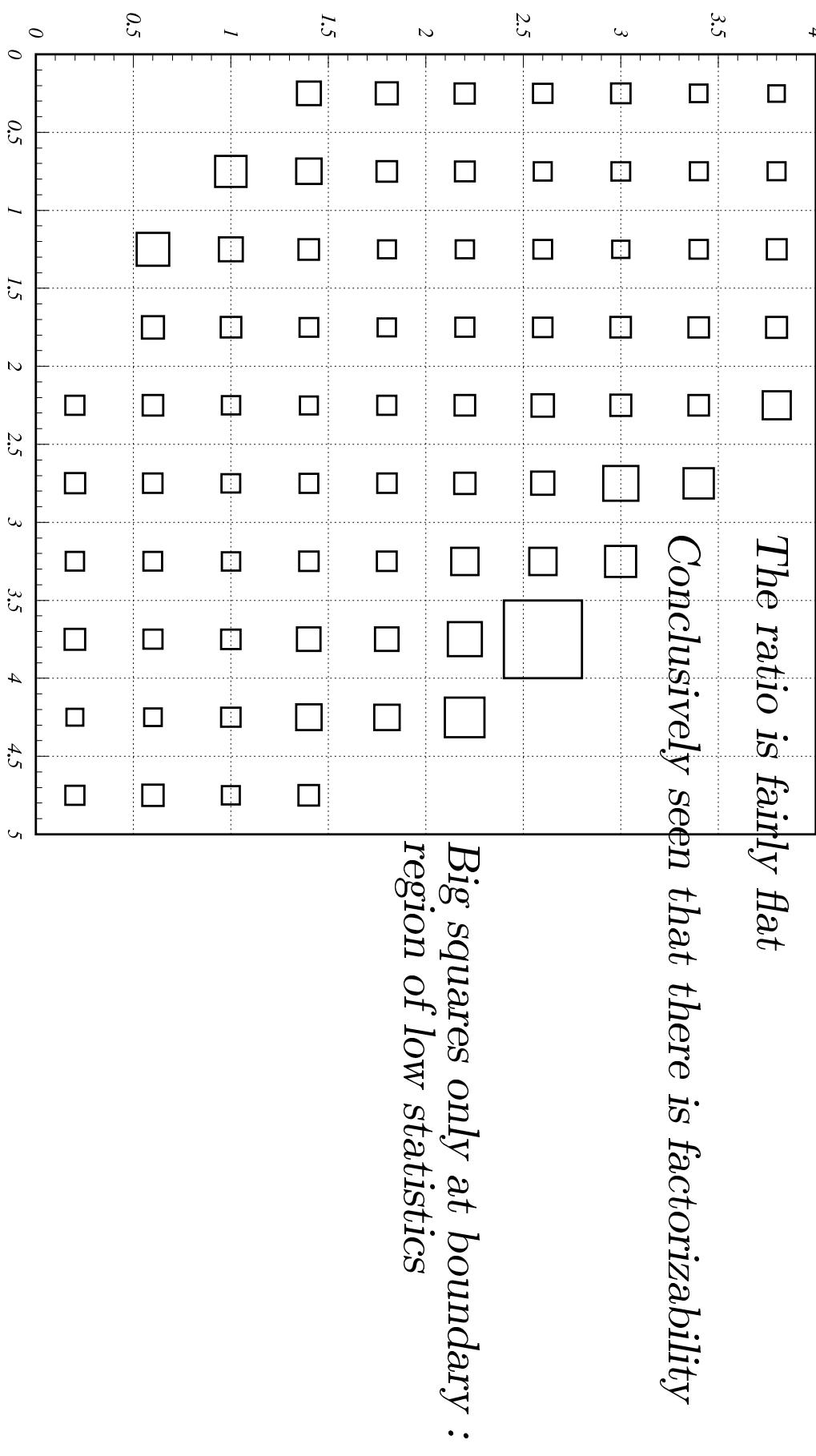
*Ratio of  $\epsilon^{D^{*+}}(p_1, p_2)$  to  $\epsilon^1(p_1) \times \epsilon^2(p_2)$  should be flat*

- We'll see that for factorizability to hold good the above ratio should be flat
- $\epsilon^{D^{*+}}(p_1, p_2, p_3) = N_3(p_3) \times \epsilon^{D^{*+}}(p_1, p_2)$ 
  - since  $p_3$  is constrained by  $D^{*+}$  kinematics, here  $N_3$  is some scale factor
  - this  $\implies {}^R \epsilon^{D^{*+}}(p_1, p_2, p_3) dp_3 = {}^R N_3(p_3) dp_3 \times \epsilon^{D^{*+}}(p_1, p_2)$
- Assume  $\epsilon^{D^{*+}}(p_1, p_2, p_3) = \epsilon^1(p_1) \times \epsilon^2(p_2) \times \epsilon^3(p_3)$ 
  - this  $\implies {}^R \epsilon^{D^{*+}}(p_1, p_2, p_3) dp_3 = [{}^R \epsilon_3(p_3) dp_3] \times \epsilon^1(p_1) \times \epsilon^2(p_2)$
- From the above  $\epsilon^{D^{*+}}(p_1, p_2) = \frac{{}^R N_3(p_3) dp_3}{\epsilon_3(p_3) dp_3} \times \epsilon^1(p_1) \times \epsilon^2(p_2)$ 
  - This means the ratio is flat

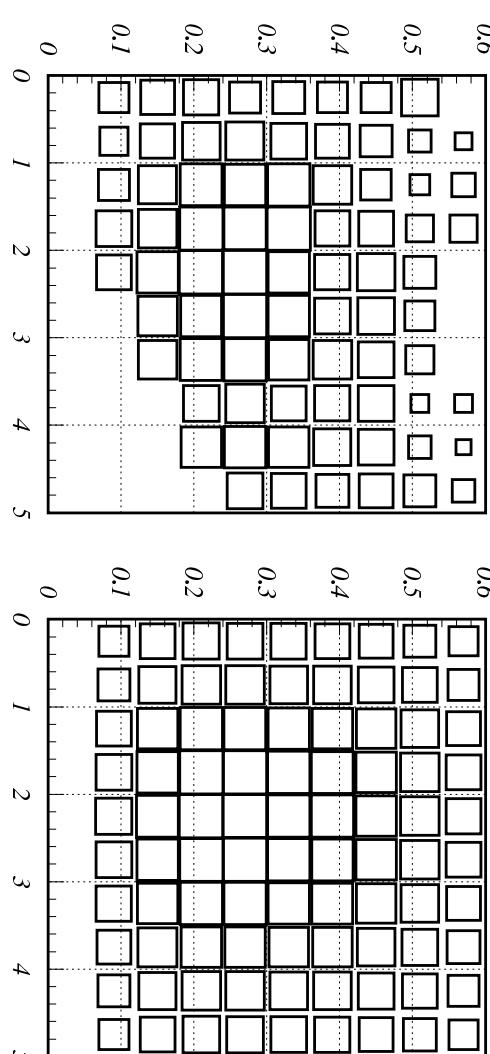
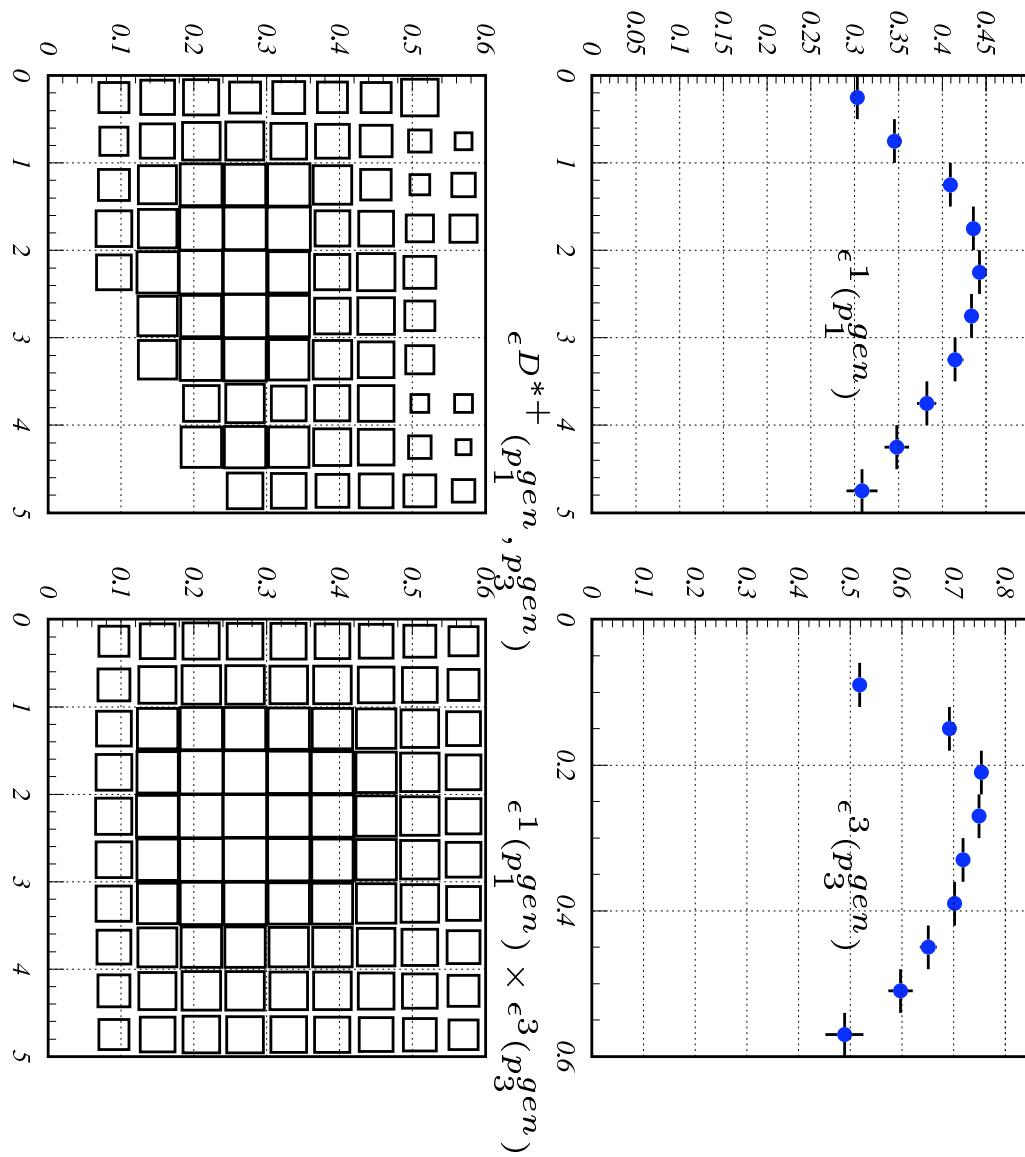
## Factorizability in $D^0 \rightarrow K_S \pi^0$



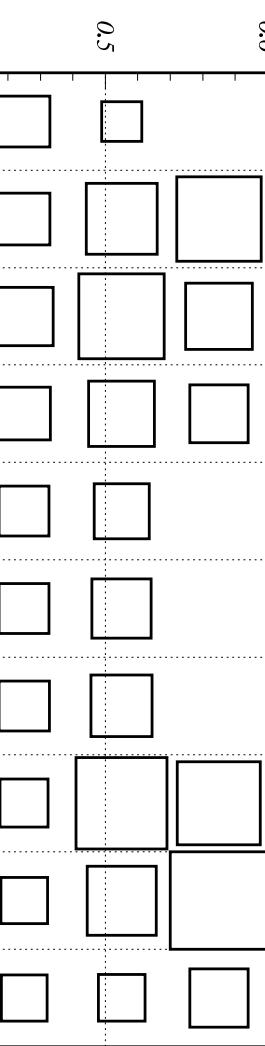
Ratio of  $\epsilon^{D^{*+}}(p_1, p_2)$  and  $\epsilon^1(p_1) \times \epsilon^2(p_2)$ , in  $D^0 \rightarrow K_S \pi^0$



## Factorizability in $D^0 \rightarrow K_S \pi^0$ continues...

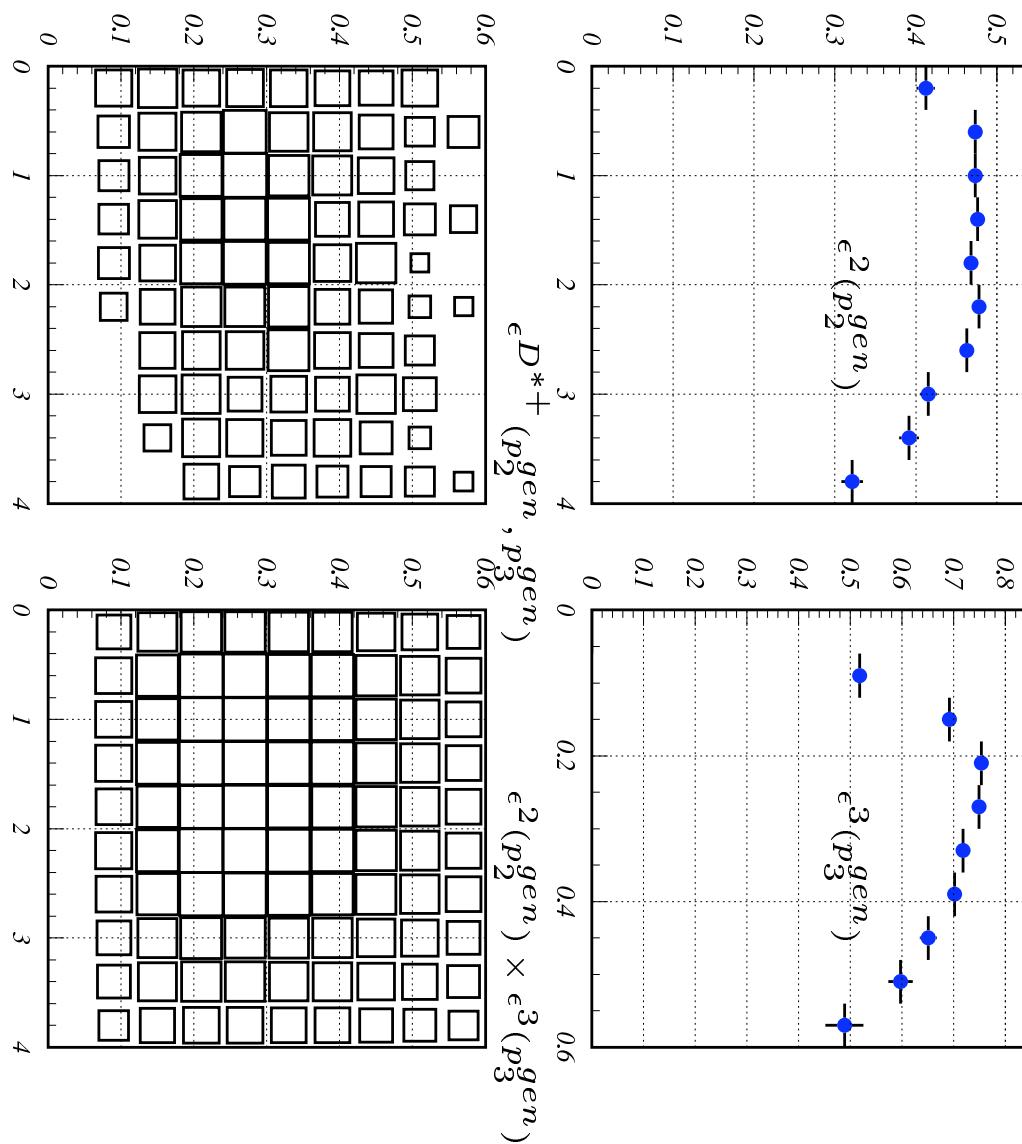


Ratio of  $\epsilon^{D^{*+}}(p_1, p_3)$  and  $\epsilon^1(p_1) \times \epsilon^3(p_3)$ , in  $D^0 \rightarrow K_S \pi^0$

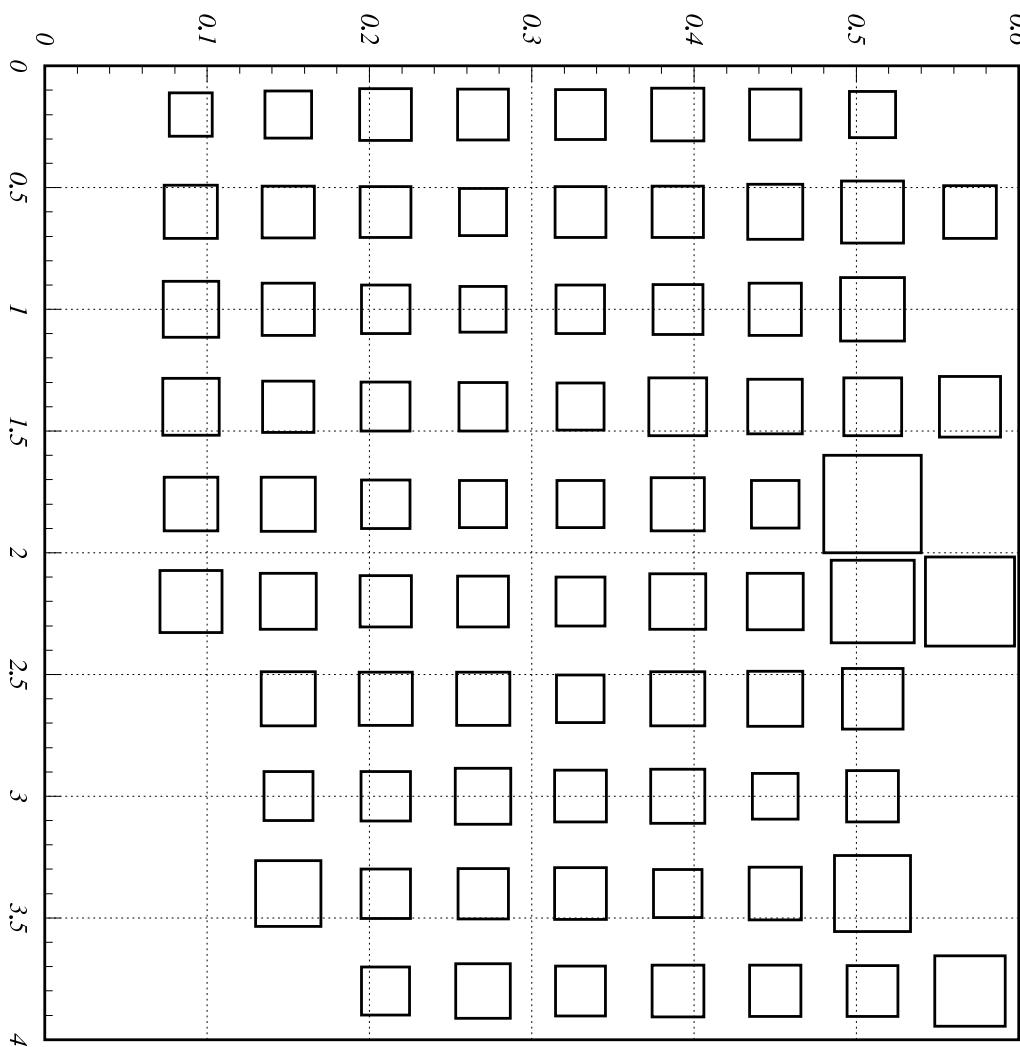


The ratio is fairly flat  
Conclusively seen that  
there is factorizability

## Factorizability in $D^0 \rightarrow K_S \pi^0$ continues...



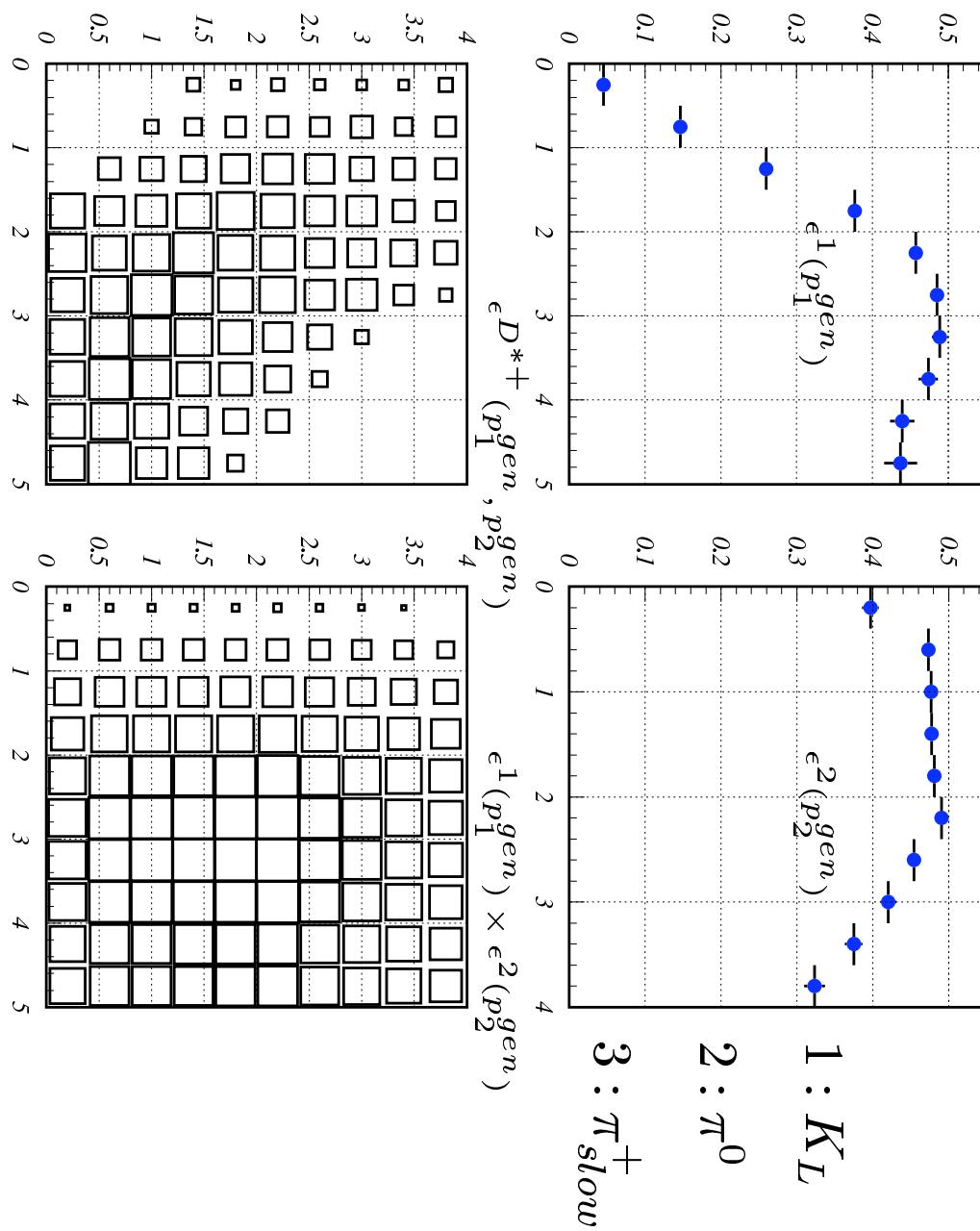
*Ratio of  $\epsilon^{D^{*+}}(p_2, p_3)$  and  $\epsilon^2(p_2) \times \epsilon^3(p_3)$ , in  $D^0 \rightarrow K_S \pi^0$*



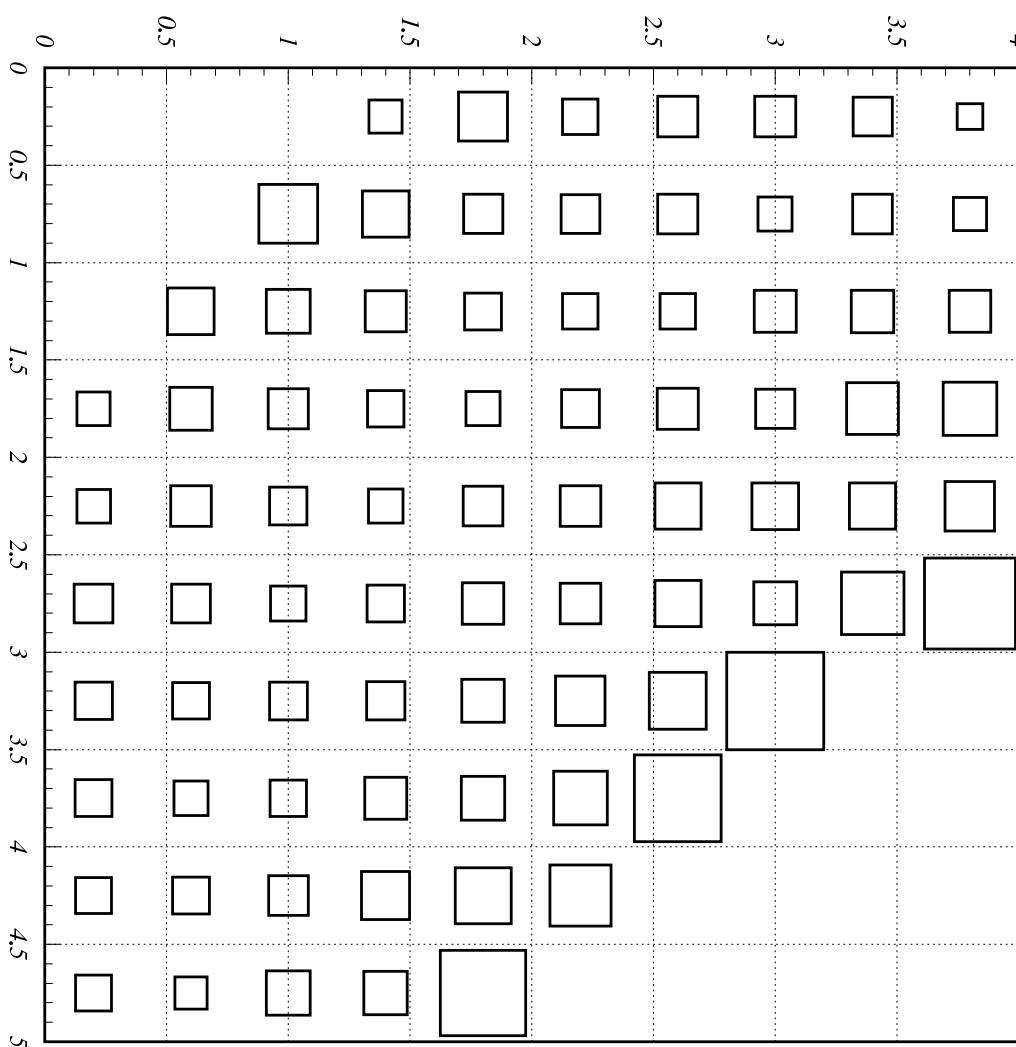
*The ratio is flat*

*There is factorizability*

## Factorizability in $D^0 \rightarrow K_L \pi^0$

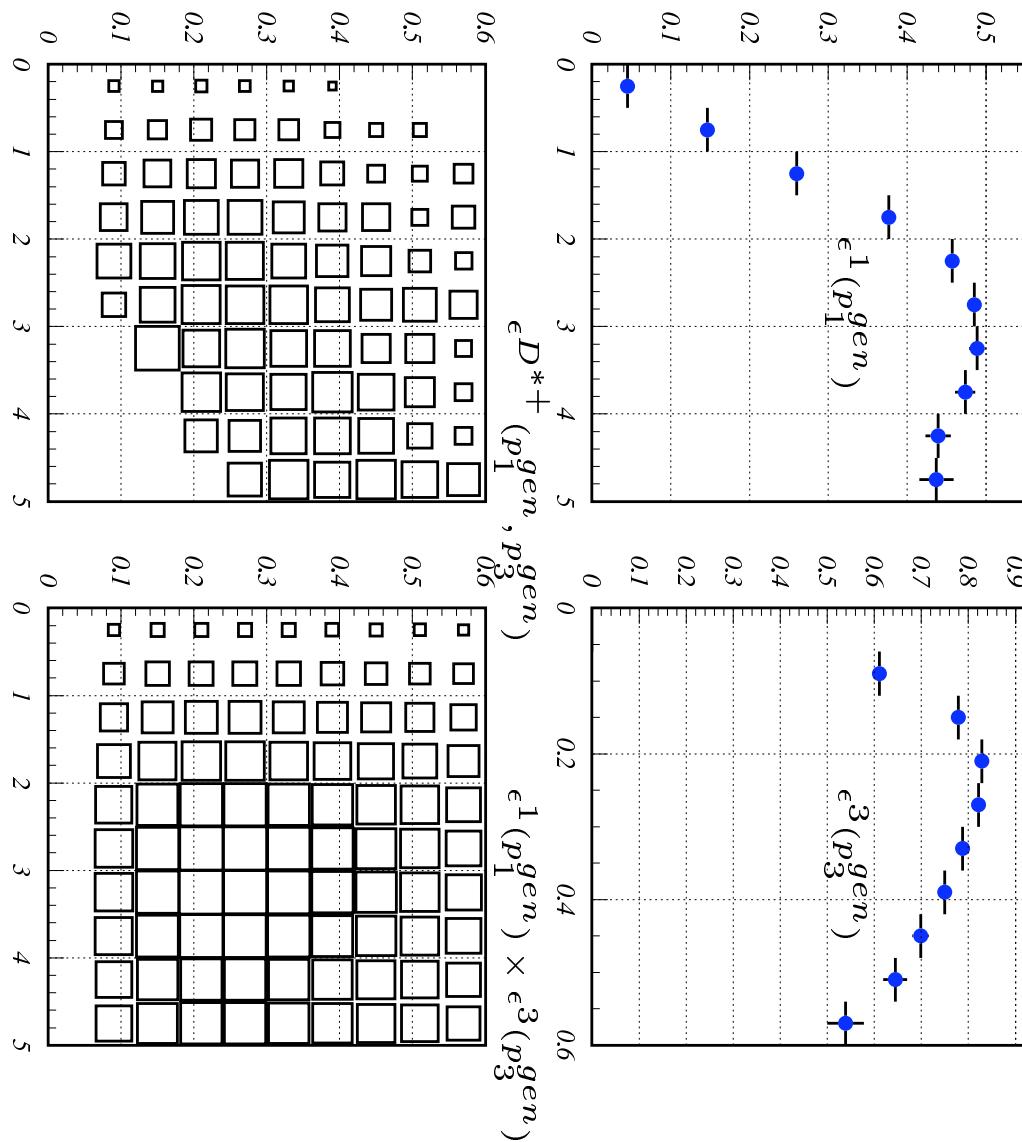


Ratio of  $\epsilon^{D^{*+}}(p_1, p_2)$  and  $\epsilon^1(p_1) \times \epsilon^2(p_2)$ , in  $D^0 \rightarrow K_L \pi^0$

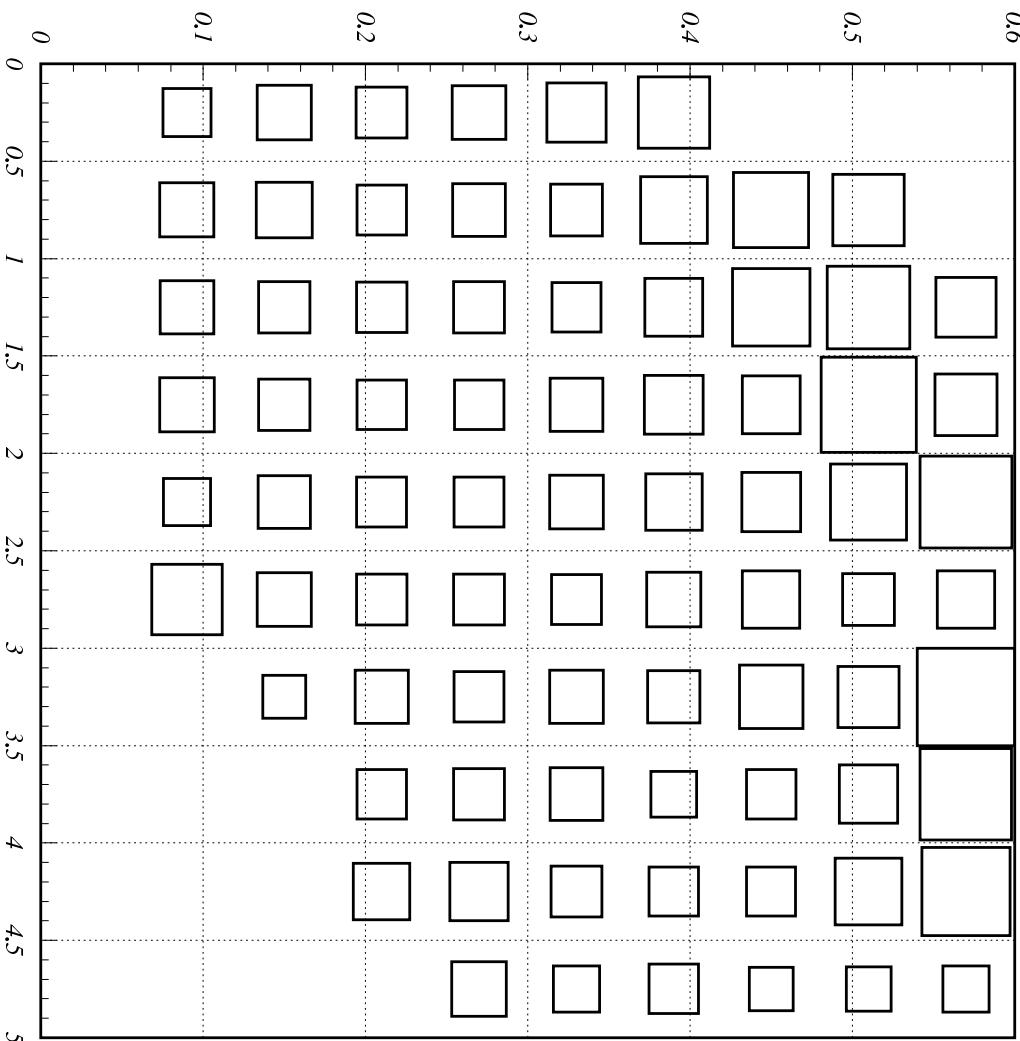


The ratio is flat  
There is factorizability

## Factorizability in $D^0 \rightarrow K_L \pi^0$ continues...



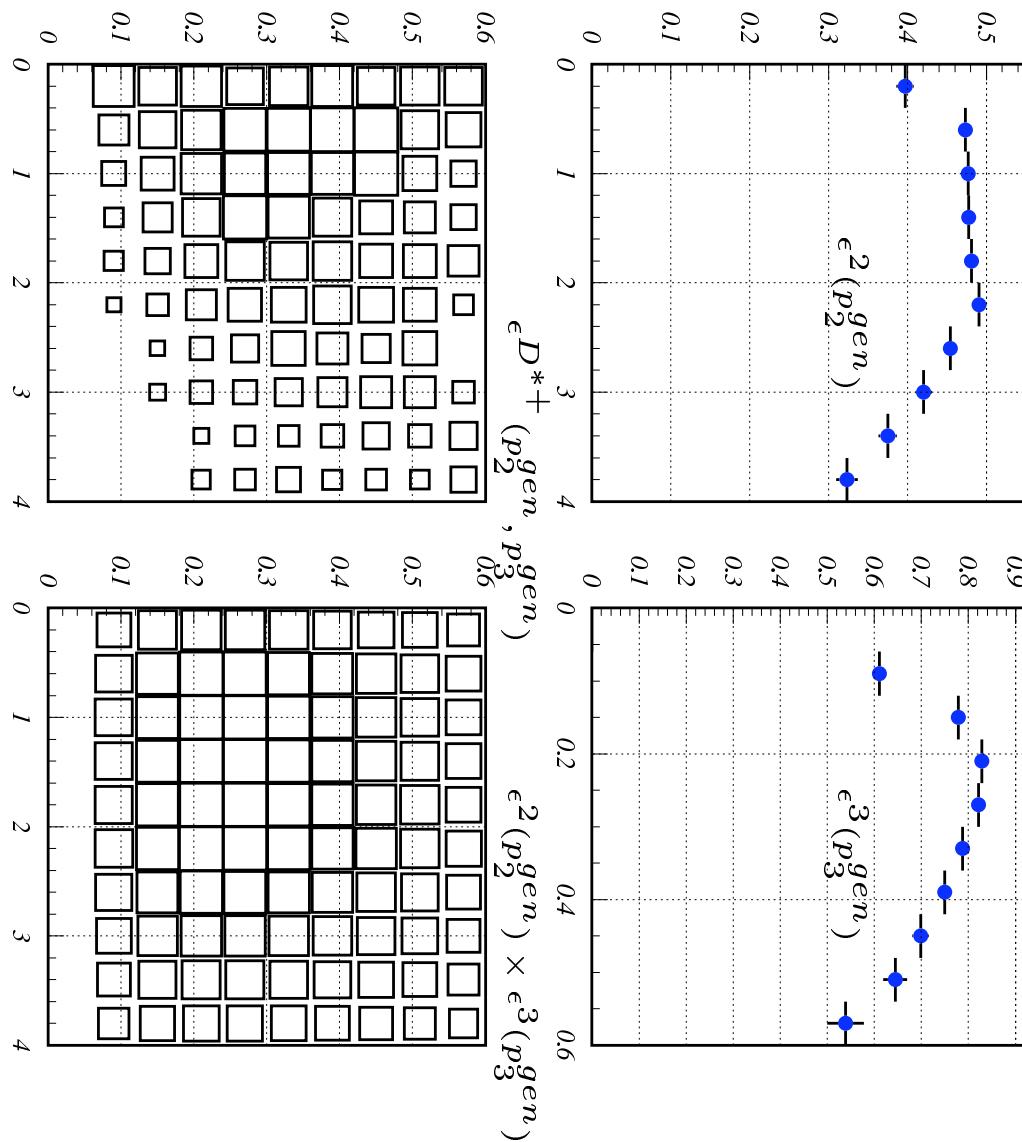
Ratio of  $\epsilon^{D^{*+}}(p_1, p_3)$  and  $\epsilon^1(p_1) \times \epsilon^3(p_3)$ , in  $D^0 \rightarrow K_L \pi^0$



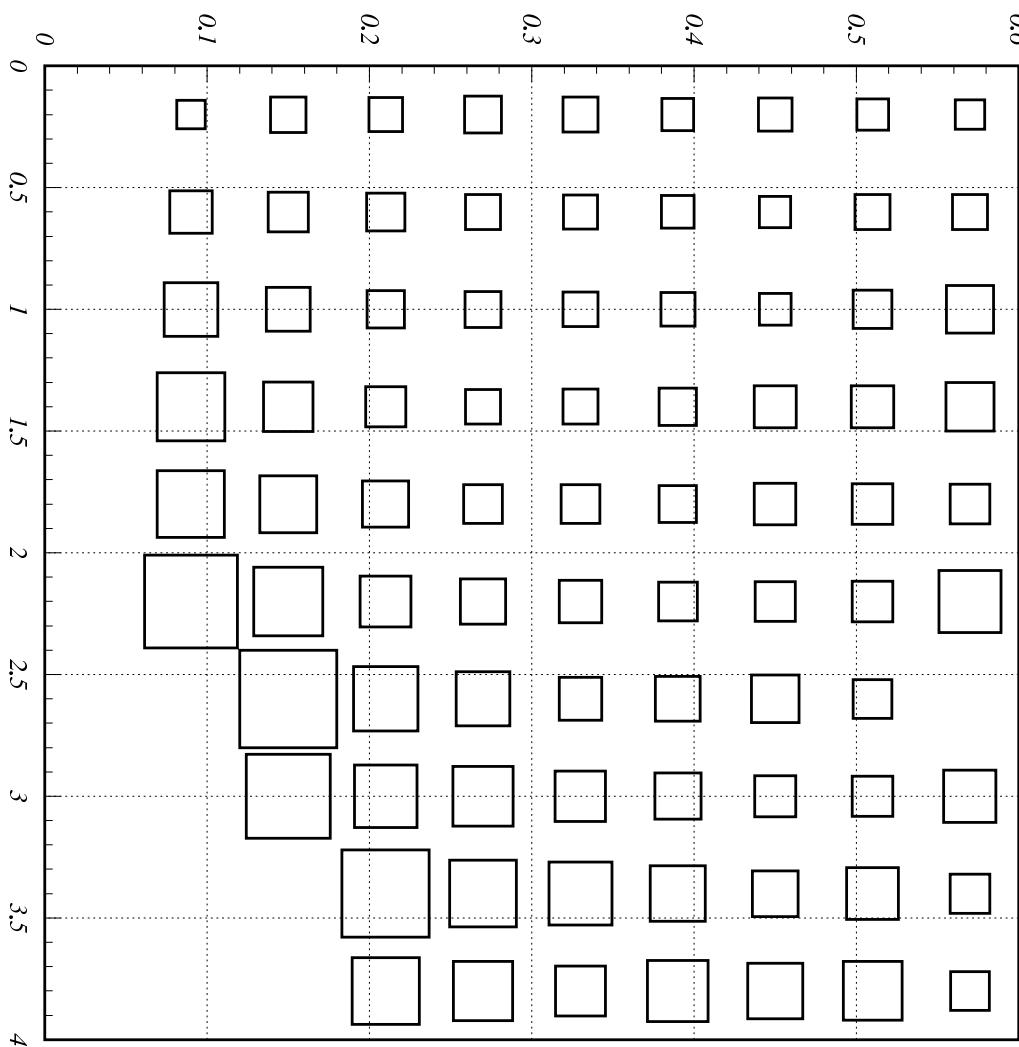
The ratio is flat

There is factorizability

## Factorizability in $D^0 \rightarrow K_L \pi^0$ continues...



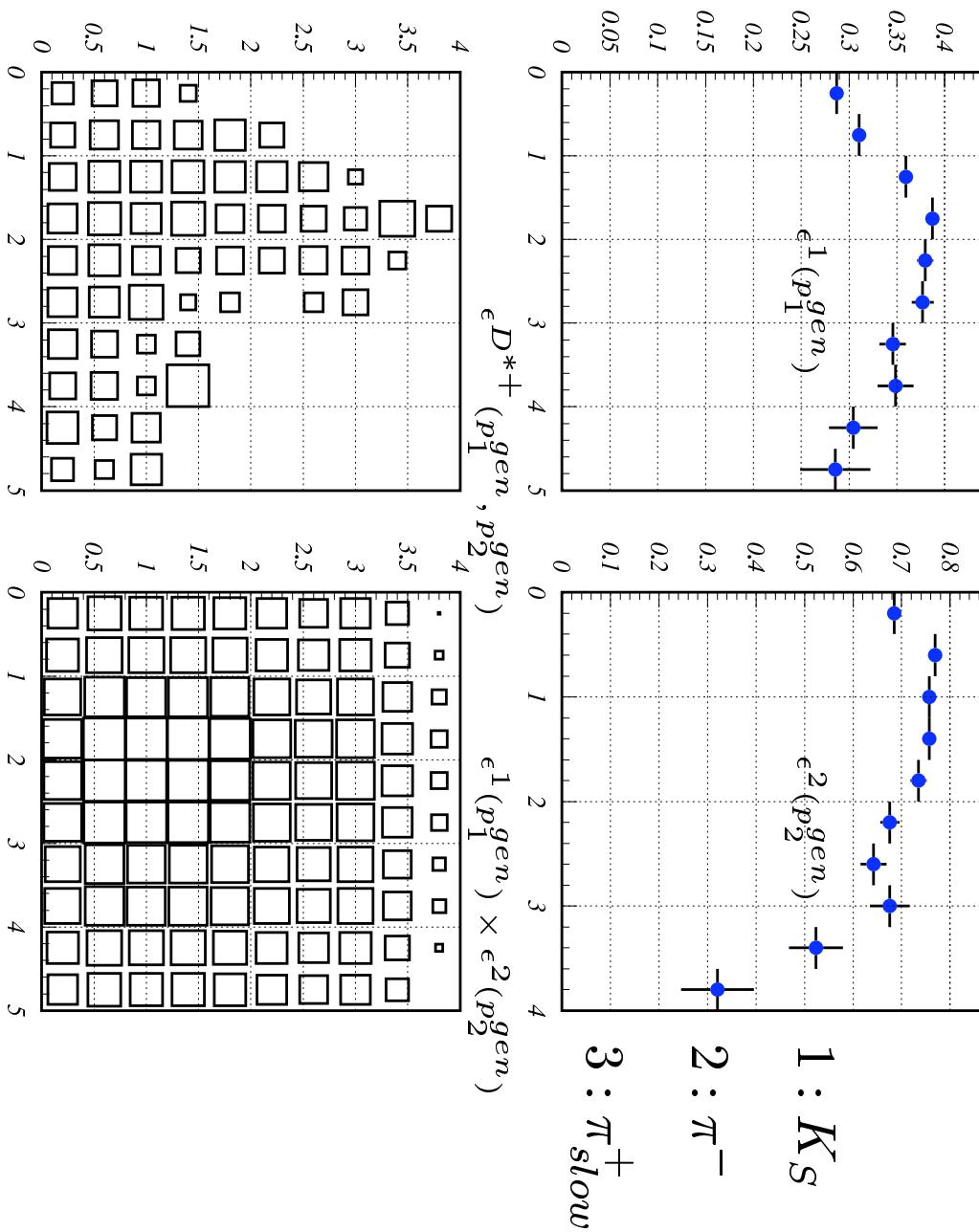
Ratio of  $\epsilon^{D^{*+}}(p_2, p_3)$  and  $\epsilon^2(p_2) \times \epsilon^3(p_3)$ , in  $D^0 \rightarrow K_L \pi^0$



The ratio is flat

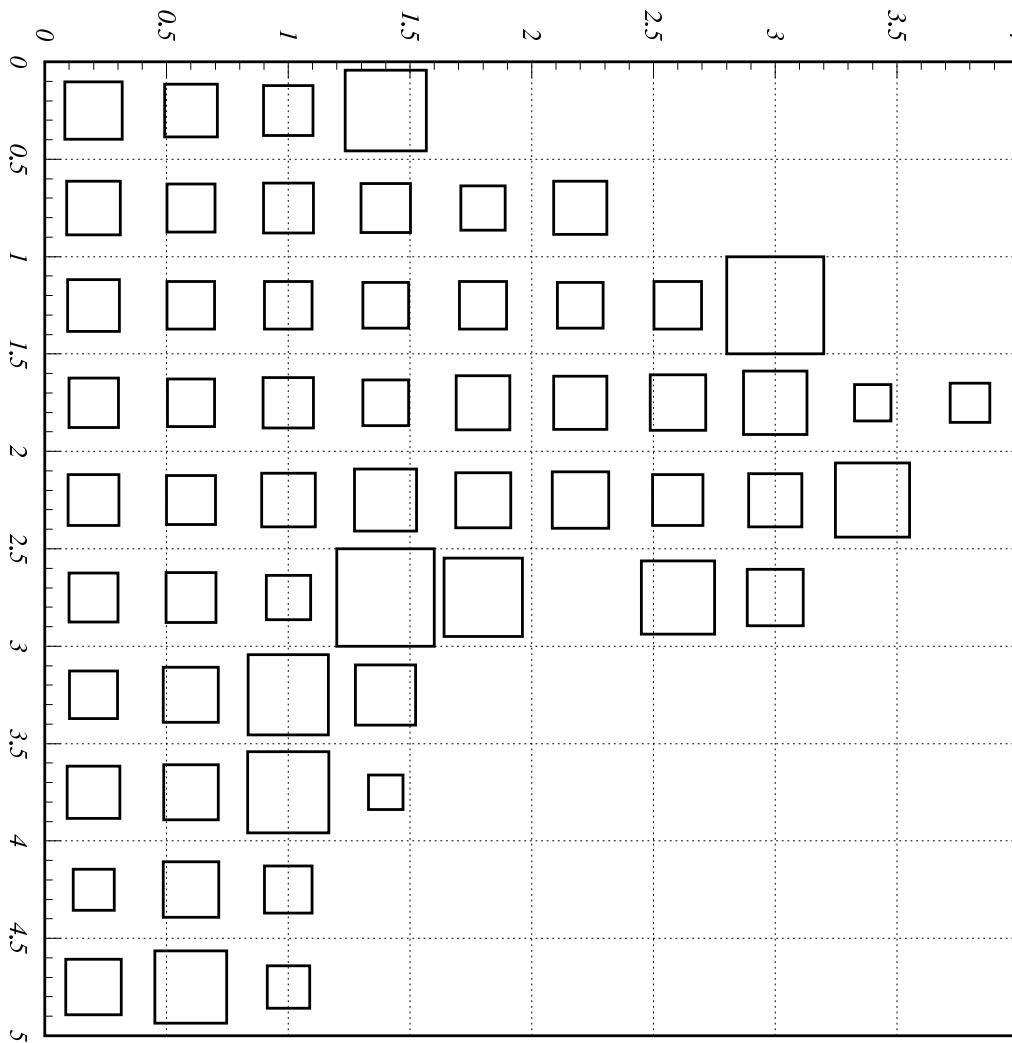
There is factorizability

Factorizability in  $D^0 \rightarrow K_S \pi^+ \pi^-$ , result shown partly, rest similar

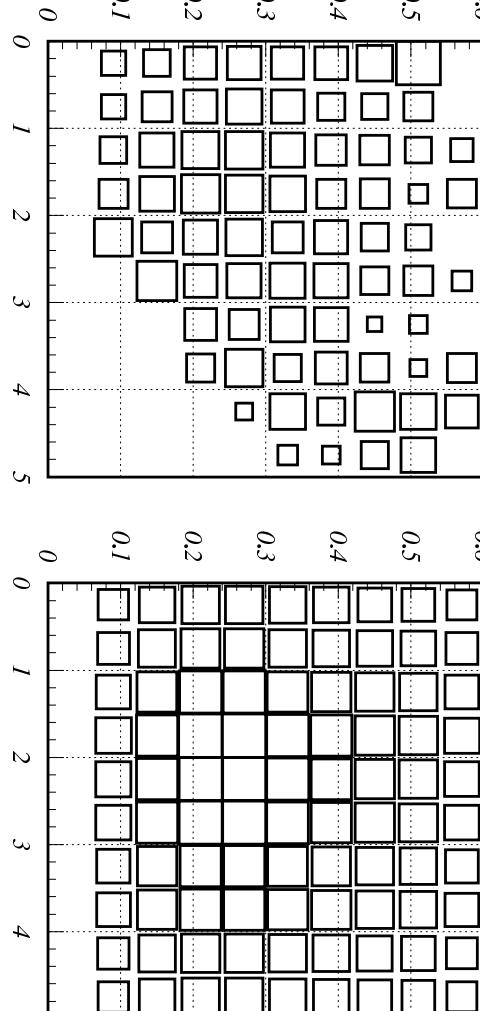
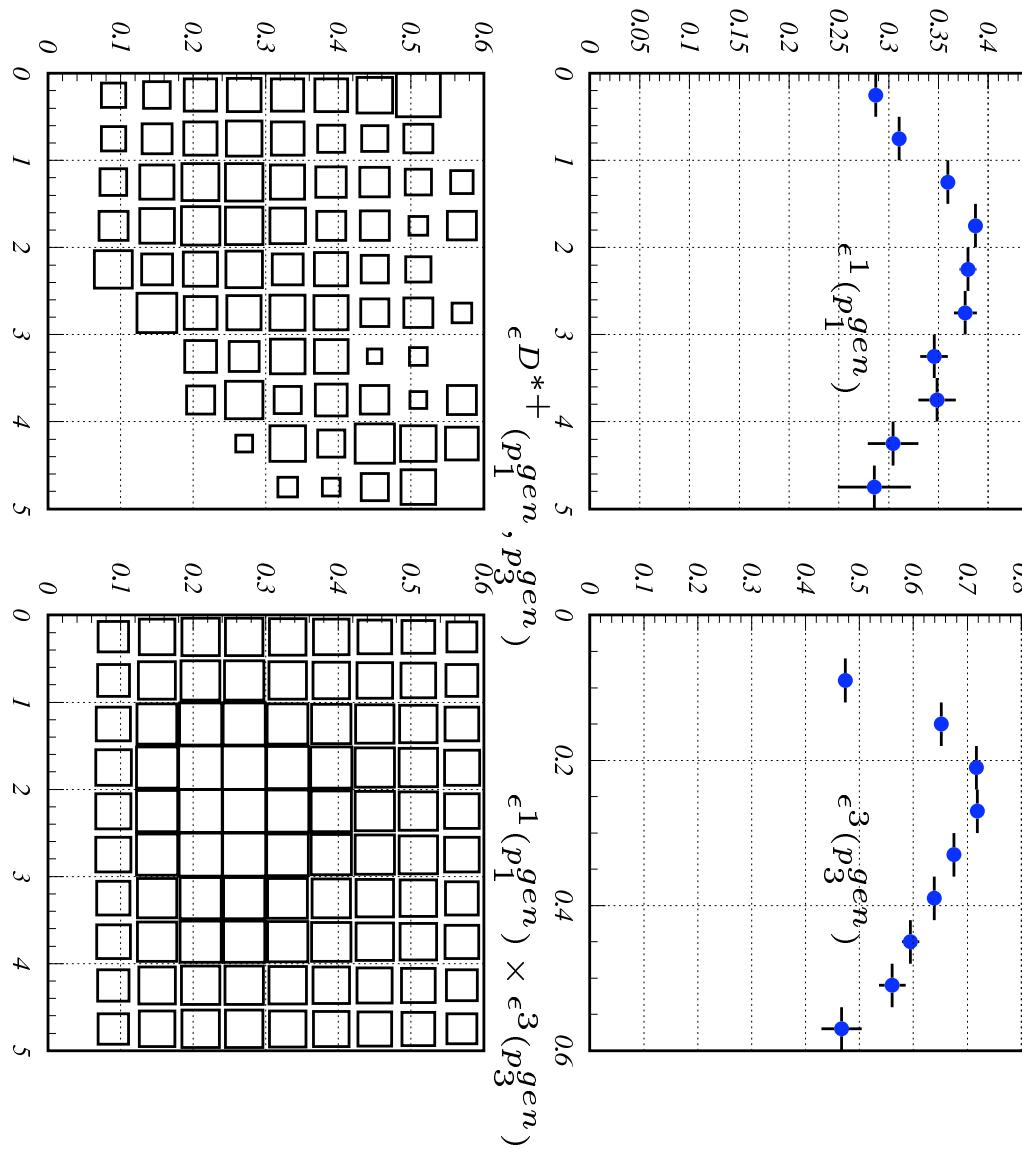


Ratio of  $\epsilon^{D^{*+}}(p_1, p_2)$  and  $\epsilon^1(p_1) \times \epsilon^2(p_2)$ , in  $D^0 \rightarrow K_S \pi^+ \pi^-$

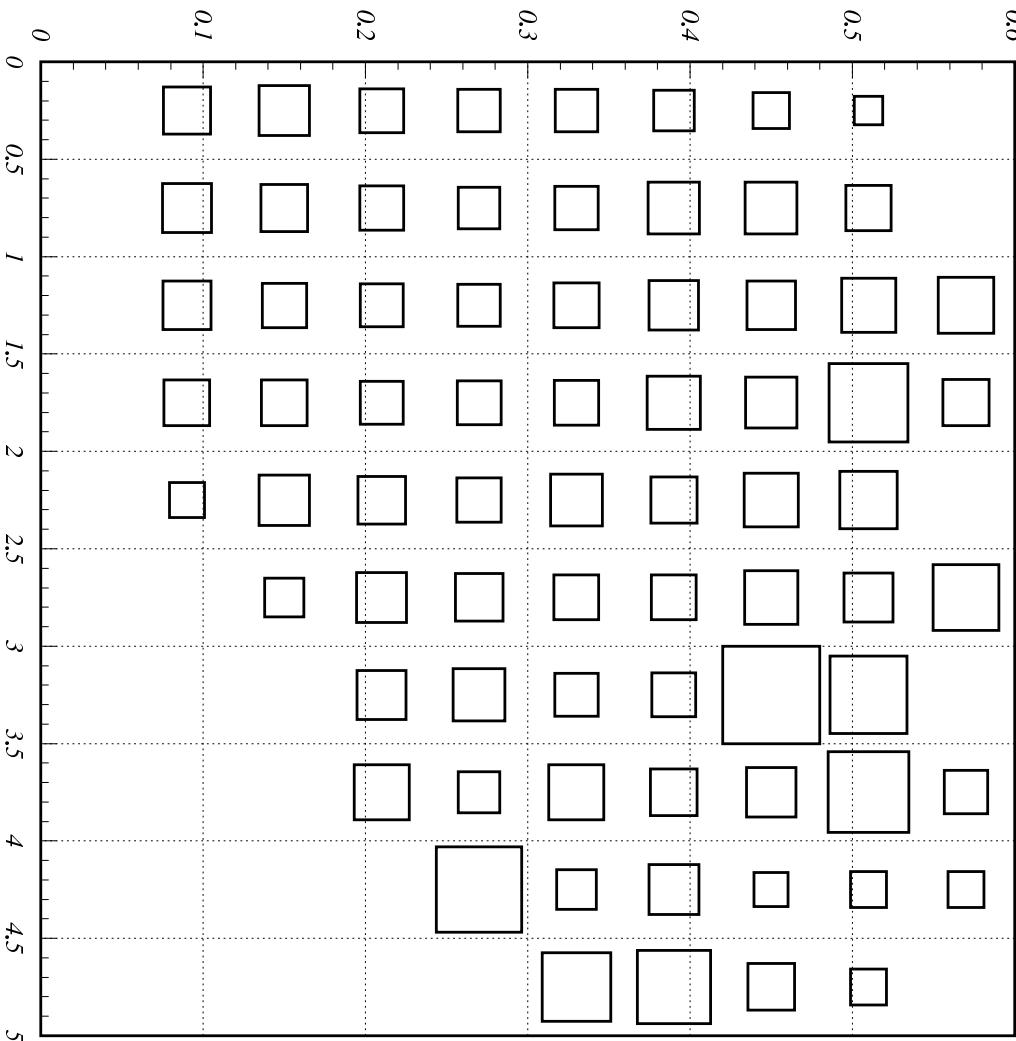
The ratio is flat  
There is factorizability



## Factorizability in $D^0 \rightarrow K_S \pi^+ \pi^-$ continues....



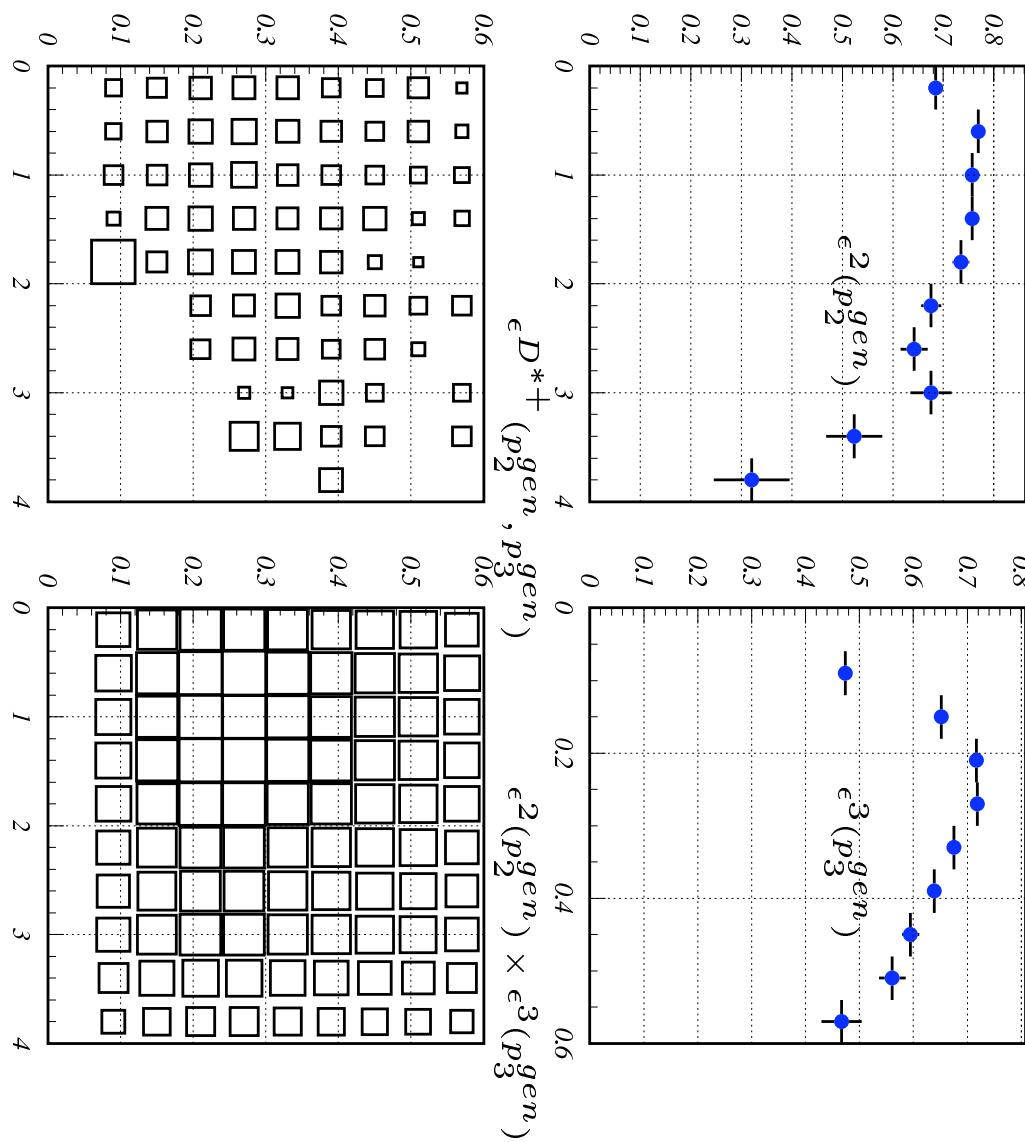
Ratio of  $\epsilon^{D^{*+}}(p_1, p_3)$  and  $\epsilon^1(p_1) \times \epsilon^3(p_3)$ , in  $D^0 \rightarrow K_S \pi^+ \pi^-$



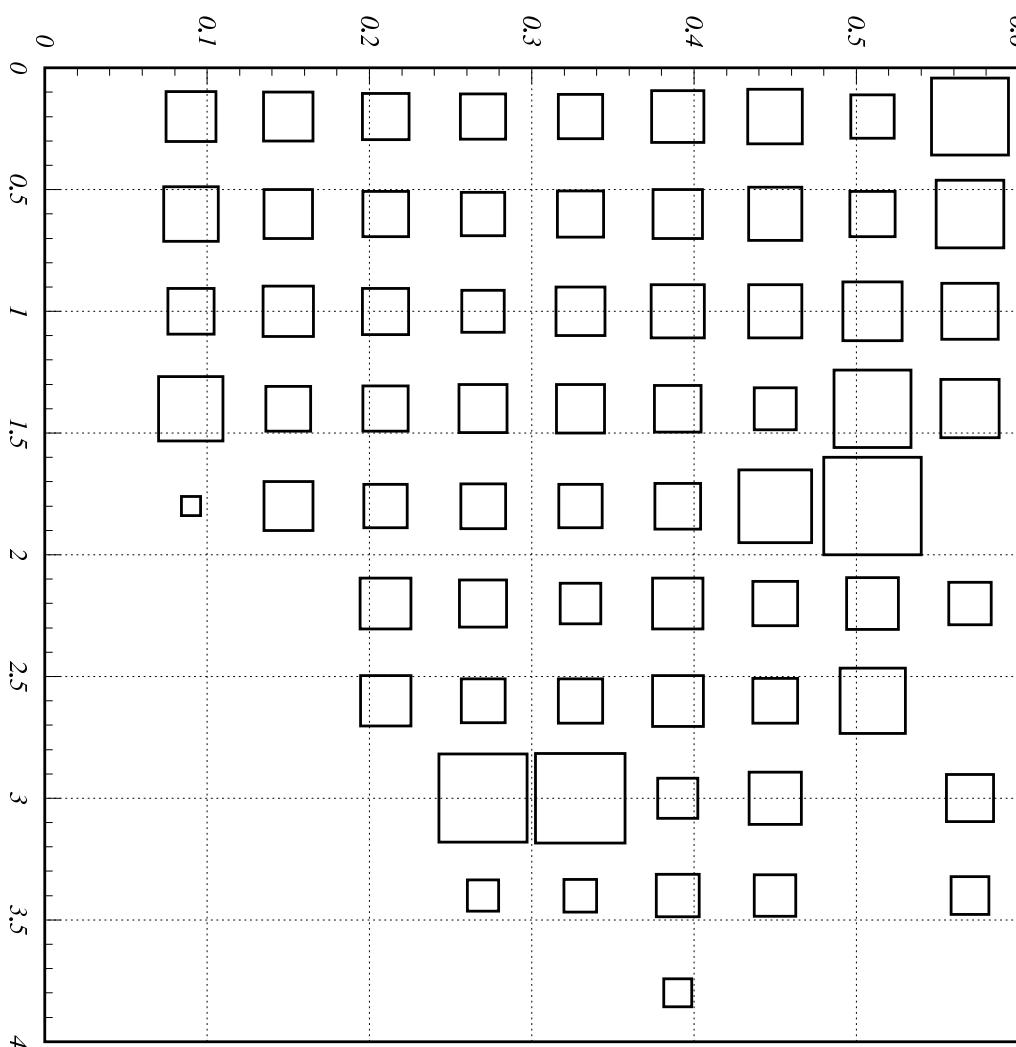
The ratio is flat

There is factorizability

## Factorizability in $D^0 \rightarrow K_S \pi^+ \pi^-$ continues....



Ratio of  $\epsilon^{D^{*+}}(p_2, p_3)$  and  $\epsilon^2(p_2) \times \epsilon^3(p_3)$ , in  $D^0 \rightarrow K_S \pi^+ \pi^-$



## Future Course

- Any improvements in efficiency study and fitting
- Add charge conjugate modes
- Skim and analyze small amount of data say  $\exp(7+9+11+13)$ ,  
 $\int \alpha dt = 32.407 fb^{-1}$ 
  - crosscheck with MC results. eg Signal and  $K^0$  momentum spectra
  - preliminary asymmetry can be calculated as all quantities will be available
  - can compare with some of Roman's results previously carried out at Belle
- Background study
- Skim and analyze available data set
- Systematics study and Final asymmetry calculation